

(12) INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(19) World Intellectual Property Organization
International Bureau



(43) International Publication Date
3 May 2001 (03.05.2001)

PCT

(10) International Publication Number
WO 01/31537 A2

(51) International Patent Classification⁷: **G06F 17/60**

Hall Lane, Gaithersburg, MD 20850 (US). **KARPISH-PAN, Sonya** [US/US]; 259 Congressional Lane, #502, Rockville, MD 20852 (US).

(21) International Application Number: **PCT/US00/29369**

(22) International Filing Date: 26 October 2000 (26.10.2000)

(74) Agents: **COHEN, Herbert** et al.; Blank Rome Comisky & McCauley LLP, Suite 1000, 900 17th Street, N.W., Washington, DC 20006 (US).

(25) Filing Language: English

(26) Publication Language: English

(30) Priority Data:
60/161,355 26 October 1999 (26.10.1999) US
09/695,046 25 October 2000 (25.10.2000) US

(81) Designated States (*national*): AE, AG, AL, AM, AT, AU, AZ, BA, BB, BG, BR, BY, BZ, CA, CH, CN, CR, CU, CZ, DE, DK, DM, DZ, EE, ES, FI, GB, GD, GE, GH, GM, HR, HU, ID, IL, IN, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS, LT, LU, LV, MA, MD, MG, MK, MN, MW, MX, MZ, NO, NZ, PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT, TZ, UA, UG, US, UZ, VN, YU, ZA, ZW.

(71) Applicant (*for all designated States except US*): **ADAPTIVE TRADE, INC.** [US/US]; 5th floor, 6 Montgomery Village Avenue, Gaithersburg, MD 20879 (US).

(84) Designated States (*regional*): ARIPO patent (GH, GM, KE, LS, MW, MZ, SD, SL, SZ, TZ, UG, ZW), Eurasian patent (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent (AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU, MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM, GA, GN, GW, ML, MR, NE, SN, TD, TG).

(72) Inventors; and

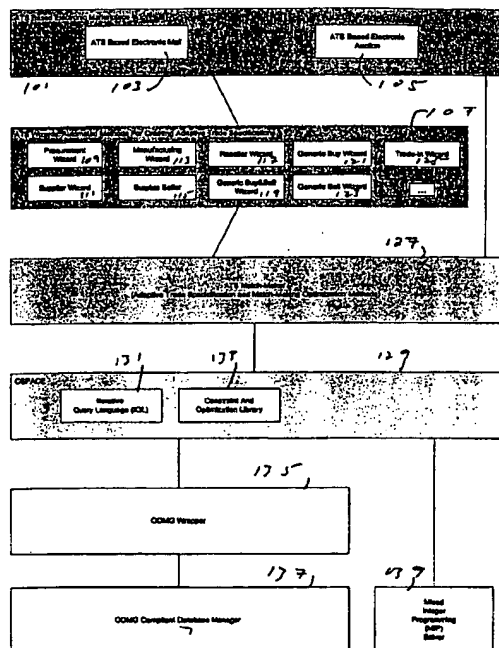
(75) Inventors/Applicants (*for US only*): **BRODSKY, Alex** [US/US]; 222 Rollins Avenue, Rockville, MD 20852 (US). **ZELIVINSKI, Stanislav** [US/US]; 11505 Brandy Hall Lane, Gaithersburg, MD 20850 (US). **KATZ, Marcel** [US/US]; 1710 Wilmart Street, Rockville, MD 20852 (US). **GOZHANSKY, Alan** [US/US]; 11505 Brandy

Published:

— Without international search report and to be republished upon receipt of that report.

[Continued on next page]

(54) Title: **SYSTEM AND METHOD FOR ADAPTIVE TRADE SPECIFICATION AND MATCH-MAKING OPTIMIZATION**



(57) Abstract: Electronic commerce is facilitated through adaptive trade specifications and matchmaking optimization. Adaptive trade specifications provide a standard format for traders to specify what they want to obtain and what they are willing to give for it, in both qualitative and quantitative terms, as well as constraints and an objective such as maximum profit or minimum price. The standard format of the adaptive trade specifications allows the matchmaking optimization process to find the optimal match between traders. For example, if a buyer wishes to minimize the price of a desired purchase, subject to certain constraints, the standard format allows location of sellers meeting the constraints and performs one of various types of optimization to match the buyer with one or more sellers. Thus, one or more mutually agreeable transactions can be recommended.

WO 01/31537 A2



For two-letter codes and other abbreviations, refer to the "Guidance Notes on Codes and Abbreviations" appearing at the beginning of each regular issue of the PCT Gazette.

System and Method for Adaptive Trade Specification and Match-Making Optimization***Cross-Reference to Related Applications***

The present application claims the benefit of U.S. Provisional Application No. 60/161,355, filed October 26, 1999. Related subject matter is set forth in U.S. Provisional Application Nos. 60/163,425 and 60/163,243, both filed November 3, 1999. The disclosures of all of the just-cited provisional applications are hereby incorporated by reference in their entireties into the present disclosure.

Background – Field of Invention

The present invention relates to a system and method for conducting trade activities and more particularly to a system and method for conducting trade activities electronically with the capability of achieving and optimizing complex trade objectives in the realm of electronic commerce.

Background – Discussion of Prior Art

Current electronic commerce systems lack the decision support capabilities necessary for achieving the objectives of the various traders, especially in business-to-business electronic transactions. For example:

- **Procurement Organization.** A business or government agency may seek to perform a multi-million dollar procurement of various office supplies from a possibly large number of authorized suppliers. An example of a procurement objective is to minimize the total expenditure on the required quantities of office supplies, under the limitations of the allocated budget, and the maximal price per specific items the agency is ready to pay. It is desirable that the underlying E-commerce system would recommend the optimal trade, i.e., what items and in what quantities should be purchased from each authorized supplier and for what price. Buying each item from a supplier offering the minimal price per item may not be the best

strategy, because of various deals, incentives and volume discounts that suppliers may be willing to offer.

• **Supplier.** A computer hardware supplier offers a range of components and their configurations. One possible objective is maximizing its revenue, while maintaining at least a 17% profit margin, subject to limitations on the current inventory levels and capacity, and under the requirement that inventory turnover be at least 50% per month. Also, a supplier may be willing to offer numerous special deals and incentives to preferred volume buyers.

• **Manufacturer.** A pharmaceutical manufacturer may seek to perform a complex transaction of selling a bundle of its products to a chain of drug stores, and, at the same time, purchasing a range of raw materials necessary to manufacture them. In doing so, the manufacturer may be trying to achieve the objective of maximizing the overall profit subject to the limitations on manufacturing production capacity, available manufacturing processes and the available cash.

• **Collaborating Bidder.** An authorized (e.g., on a GSA schedule) supplier (or manufacturer) is willing to put a bid in response to a big procurement solicitation by the federal government. The supplier may be too small to respond to large-scale solicitation, and he may seek to find a bidding alliance with other complementary suppliers. An example objective of the supplier may be to minimize the combined bid price (to increase the chances of winning), while guaranteeing his own 13% profit margin and under the restriction that his expenses shall not exceed \$2 million.

• **Surplus Seller.** An electronic device manufacturer may seek to eliminate useless surplus inventory. The objective here may be to maximize the sale price for the overall surplus, possibly selling it to more than one buyer.

For decision support, corporations with large volume of business transactions maintain extensive operations and R&D staff, as well as special-purpose, often proprietary, decision-

support systems. However, the development of such special-purpose systems requires tremendous R&D effort in terms of time and capital outlay. Furthermore, those special purpose systems are typically not adaptable when it comes to dynamic evolutionary changes in business structure, constraints and objectives. Moreover, even in large corporations, many of the decision support activities, such as in the above examples, are not automated. Most importantly, special purpose systems are not capable of supporting transactions that span across widely distributed suppliers, manufacturers, and procurement organizations. On the other side of the spectrum, many small and medium size companies and organizations simply cannot afford the luxury of maintaining large sales and procurement staff and the special-purpose decision support tools. Those companies cannot keep up with ever-changing business opportunities, which often involve numerous business parties engaged in electronic commerce.

Companies such as Ariba, CommerceOne, Commerce Exchange, etc., do provide procurement and supply side integration, but the decision of exactly which items need to be purchased or sold, from or to which trader, and in what quantities and for what prices is left to sales and procurement personnel. Also lacking matchmaking optimization capabilities are Internet-based electronic commerce services, such as electronic malls and shops (e.g., IMALL and Amazon.com), electronic auctions (e.g., EBAY and Yahoo), and competitive shopping (e.g., PriceLine.com, using a reverse auction). Today, companies in that category mainly provide business-to-consumer and consumer-to-consumer services, but are also trying to expand into the business-to-business market. Products like IBM Net.Commerce and MS Site Server are suites of software productivity tools used to deploy a wide range of E-commerce solutions. However, they also lack the decision support capabilities necessary for achieving complex trade objectives.

Current Internet-based trade systems only support simple trade objectives such as purchasing or selling specific items within a certain price range. For example, EBAY allows the auctioning of specific items, i.e., iterative price-bids bounded by a floor price and a time deadline. IMALL supports selling specific products or services at a fixed price.

5 PriceLine.com allows customers to bid their own price for a product or service, does comparative shopping and keeps the monetary difference.

Prior art examples of systems and methods used in connection with electronic commerce, trade optimization and logistics support are disclosed in various US Patents and related literature.

10 US Patent No. 4,903,201 discloses a computerized automated *futures trading exchange*. The traders in the exchange enter bids to purchase commodity contracts. They also enter offers to sell commodity contracts. The system automatically matches between bids and offers. The system automatically completes transactions between traders.

The invention above lacks the capability to match an aggregation of partial bids to an

15 aggregation of partial offers, where bids and offers are specified as ranges delimited by constraints. In the invention above the trader lacks the capability to define an objective function and to perform optimization on the specified objective function. The invention above is limited to the *futures* markets.

US Patent No. 5,077,665 discloses a matching system in which bids are automatically

20 matched against offers for given trading instruments. Although the system provides match making between bids and offers of financial instruments, the system does not provide the trader the ability to specify objective function, to set constraints per specific financial instrument, and therefore to achieve a predefined business objective. The invention described therein is related only to financial markets and does not allow the user to specify other items

25 for match making besides financial instruments.

US Patent No. 5,283,731 discloses computer-based classified advertising. The system comprises a data processor and means for creating an advertising database available to each user in the system. The invention described therein restricts the matching capabilities to a single match and does not provide capabilities to perform optimization and to specify
5 complex trading specifications, constraints and objectives.

US Patent No. 5,710,887 discloses a computer system and method for electronic commerce. The system facilitates commercial transactions between a plurality of customers and at least one supplier of items over a computer driven network capable of providing communications between the supplier and at least one customer site associated with each
10 customer. Despite the fact that the system disclosed in the invention is suitable for a wide range of providers of goods and services, it does not possess the ability to specify particular items in a precise way, or to perform optimized match making. The invention described therein describes various business paradigms for electronic commerce, but does not allow performing "One-to-one" or "One-To-Many" electronic transactions based on optimized
15 match making. In addition, the invention described therein does not allow specification of constraints on specific item parameters.

Another area within the prior art describes various optimization methods and systems, using mostly linear optimization methods. These inventions, although providing optimization tools for business transactions, do not allow users to specify parameters of traded items in a
20 flexible way, do not allow specifications of constraints on specific parameters of a traded item, and do not allow users to perform One-to-One, and One-to-Many transactions.

US Patent No. 5,630,070 discloses the method for optimization of resources planning. The method described in the invention provides for an optimization of a manufacturing process by designating the amounts of various manufactured products to be produced. In
25 order to accomplish optimization, the method employs an objective function such as

maximization of income in a situation where there are limitations on the inventory of raw materials and on the tools employed in the manufacturing process. The method does not allow specifying unique constraints on specific items participating in the manufacturing process. The method does not allow performing multiple transactions and does not allow performing match making of consumers' items with suppliers' items.

All previous inventions describing various methods for manufacturing logistic decision support receive as input a bill of materials or a predefined set of the goods or subassemblies. They do not offer the flexibility of choosing different vendors of subassemblies through a sophisticated match making mechanism.

US Patent No. 5,450,317 discloses a method and system for optimized logistics planning. The invention described therein recommends optimal order quantities and timing, choice of vendor locations and storage locations, and transportation models, for individual items and for product families. The invention does not allow using a match making mechanism to select vendors. The invention allows for specification of fixed parameters for customers and suppliers, rather than parameters expressed through constraints.

Summary of the Invention

Summarizing the examples of the inventions described above, it is clear that none of them provides a unified way to perform optimized match making trading activities in the realm of electronic commerce. It is, therefore, an object of the invention to provide an Adaptive Trade Specification (ATS) model for using in electronic commerce realm.

It is further object of invention to provide an ATS based match making and optimization automated method that can find optimal trade transaction for variety of users in electronic commerce domain.

It is an advantage of the invention in comparison with prior art that match making and optimization are combined under one ATS based mechanism which allows traders to design

transactions that are optimal in terms of trader's objectives and which are mutually agreeable with available trade specifications

The invention allows various traders to achieve optimal trade transactions. First, it provides the Adaptive Trade Specification (ATS) model. The ATS model allows to describe, in a precise and uniform way, trade parameters, constraints and objectives for a wide range of traders, including procurement organizations, suppliers, manufacturers, resellers, surplus sellers, trade-in sellers, stock market traders, general buyers and sellers, etc. Second, given a trader's ATS, the invention provides an automated process that recommends specific transactions with other traders' ATS's, that are mutually agreeable with, and optimize the objective of, the trader's ATS (e.g. minimal price, maximal profit, etc.). More specifically, the invention comprises the following components:

- **Adaptive Trade Specification (ATS) Model.** Adaptive Trade Specification (ATS) is a formal mathematical description of trader's objective and constraints, such as in the examples in the prior art section. ATS constraints include restrictions (on quantities, prices, totals, profits, revenues etc.) that must be satisfied to perform an optimal transaction, and the interconnection between various business parameters (such as profit, quantities, prices and costs). The core of each ATS is a specification of "items" the trader offers to GIVE as well as "items" to TAKE in return. For example, a procurement organization may offer to GIVE the "item" *money* and wants to TAKE items of *office supply*. An office equipment supplier may have an ATS, in which all its catalog appears as GIVE items, and money as the only TAKE item. Whereas, a manufacturer may have an ATS, in which all of its products appear as GIVE items, all raw materials and money (i.e., revenues for its products) as TAKE items. ATS is adaptive in that various numeric parameters such as quantities of items, prices, profit, revenue, totals etc. are not fixed, but could vary, provided that they satisfy the ATS constraints. Item specifications in an ATS are also constraint-based and not fixed. For

example, an ATS of a trader may include, as one of the TAKE item specifications, a hard disk that has at least 12 GB capacity and is compatible with a G7305E mother board; no exact model or vendor is necessary. The ATS model provides a uniform and expressive way to capture any conceivable trades that can be formulated in terms of given and taken items.

5 To help traders in the definition of an ATS, a library of specialized wizards (i.e., specialized “smart” interface templates) can be used for various types of traders (e.g., suppliers, procurement organizations, manufacturers etc.), as in the examples in the Prior Art section. For each type of trader, the wizard would automatically construct an ATS from the user given set of trading parameters relevant to a trading scenario. The trader who uses a wizard would
10 not need to understand the mathematical description of an ATS, but rather trading parameters and concepts that are familiar to the trader (e.g. availability, quantity, price, revenue, etc.). However, the description of wizard library is described elsewhere in a complementary patent application cited above, and is not intended as a limitation on the present invention.

- **ATS-based Match Making (MM) Optimization Methods.** Given a trader’s ATS, the
15 MM optimization methods recommend specific transactions with other traders (i.e., against their ATS’s) that are mutually agreeable and optimize the objective of the trader’s ATS (e.g., minimal price, maximal profit etc.). The recommended set of transactions will indicate exactly with whom the transaction should be made, the exact GIVE and TAKE items and their quantities, as well as other relevant parameters (e.g., price and profit). For example, for
20 a procurement ATS (i.e., that originates from a procurement trader), the MM optimization methods recommend a set of suppliers’ ATS’s and the exact quantities of the items to be purchased from each, so that the procurement ATS objective, say the minimal total cost, is achieved. Or, for a manufacturer’s ATS, the MM optimization methods can recommend a set of ATS’s of buyers interested in the manufacturer’s products, and a set of ATS’s of suppliers
25 of raw materials, which are necessary to manufacture the products, so that the manufacturer’s

objective, say maximal profit, is achieved. The ATS-based match making and optimization are generic and work uniformly regardless of a specific wizard (or trader type) that generated them. Four exemplary MM optimization methods are set forth herein: 1. generic MM optimization with any number of committed ATS's and one optimization objective; 2. One-to-All MM optimization which has one optimizing ATS (i.e., whose objective is used for optimization) and which recommends a (multiple) transaction that may involve some or all of the committed ATS's; 3. One-to-One MM optimization, which has one optimizing ATS and recommends a transaction that may involve exactly one committed ATS; and 4. One-to-K MM optimization, where K is an integer number, which has one optimizing ATS and which recommends a multiple transaction that may involve K or less committed ATS's.

Brief Description of the Drawings

A preferred embodiment of the present invention will be set forth below with reference to the drawings, in which:

FIG. 1 *ATS-Based Trading Software System*, describes a high level graphical summary of the suite of software tools related to the ATS-Based Trading Software System.

FIG. 2 *ATS-Based Match-Making and Optimization Hardware Architecture Diagram*, describes a high level graphical summary of the hardware architecture of the system.

FIG. 3 *Item Specification and Adaptive Trade Specification (ATS) Class Diagram*, presents a high level graphical summary of the Item Specification and Adaptive Trade Specification classes.

FIGS. 4A-4E *Functional Diagram of Match-Making and Optimization Method*, present a high level graphical summary of five Mathematical Programming Optimization Methods used by the system.

FIGS. 5A-5E *Flow Charts of Specific Match-Making and Optimization Methods*, present in greater detail the methods of Figs. 4A-4E.

Detailed Description of the Preferred Embodiment

A preferred embodiment of the present invention will now be set forth in detail with reference to the drawings, in which like reference numerals refer to like elements throughout.

Fig. 1 shows an overview of the operations carried out by the preferred embodiment.

5 An ATS-based electronic marketplace 101 can include one or more of an ATS-based electronic mall 103, an ATS-based electronic auction (forward or reverse) 105, and any other ATS-based commerce environment. As noted above, participants in the marketplace 101 form ATS's through various techniques. One such technique is the use of wizards 107, including one or more of a procurement wizard 109, a supplier wizard 111, a manufacturing
10 wizard 113, a surplus seller wizard 115, a reseller wizard 117, a generic buy and sell wizard 119, a generic buy wizard 121, a generic sell wizard 123, a trade-in wizard 125, and other wizards adapted to specific purposes. These wizards, like those wizards that are known in the programming art, are utilities that guide a user through a specific task.

The ATS's formed through use of the wizards 107 are input to the ATS match-maker
15 127, which uses matchmaking optimization methods to be described below.

The processes performed by the matchmaker 127 are object-oriented and follow the specifications of the ODMG (Object Database Management Group). A Constraint Object
Oriented Database (CSPACE) 129 uses an iterative query language (IQL) 131 and a
constraint and optimization library 133 to perform the matchmaking and optimization. The
20 CSPACE 129 communicates through an ODMG wrapper 135 with an ODMG-compliant
database manager 137 and also communicates directly with a mixed integer programming
(MIP) solver 139.

The above is implemented on a hardware architecture that will now be explained with
reference to Fig. 2. The hardware architecture capable of running an ATS based match-
25 making and optimization system includes several logical tiers, each one performing specific

computational tasks. Each tier can be described in terms of specific tasks that it performs. From the hardware perspective, each tier can be built from computers having sufficient computational power.

Tier 1 includes a database server 201, which is a power server machine (preferably dual or quad Pentium III machine) running one of the following network operating systems: Windows NT 4.0, Novell 5.0, UNIX. The database server 201 performs all tasks related to data persistency, data integrity and querying. The database server 201 runs one of the commercially available object oriented databases such as Poet, Objectivity, Object Store, etc.

Tier 2 includes the application server 203, which is a power server machine (preferably dual or quad Pentium III machine) running one of the following network operating systems: Windows NT 4.0, Novell 5.0, UNIX etc. The application server 203 performs all tasks related to performing ATS-based match-making and optimization. The data are passed between layers via RMI , CORBA, DCOM or any other distributed computing protocol allowing remote method invocation and data transmission.

Tier 3 includes a Web server 205, which is a computer that responds to requests from Web browsers via HTTP. The Web server 205 transfers text files and corresponding graphics and data via HTTP to remote computers that are running Web browsers. The Web server 205 should have the functionality commonly associated with e-commerce Web servers, such as CGI (Common Gateway Interface) for performing searches and other dynamic HTML functions and SSL (Secure Socket Layer) for handling secure transactions.

The servers 201, 203, and 205 communicate with another through an internal network. However, in order to be useful to users, the Web server 205 communicates via the Internet 207 or another publicly accessible network with Tier 4, which includes computers 209 running on users' premises and used as Web clients. The Web clients 209 are computers or other devices (such as WAP-enabled wireless devices) capable of running any standard

off-the-shelf browser. The clients 209 run Web-based applications that will use information provided by the application server 203 and the Web server 205.

In the description of the model we use object-oriented programming terminology. However, the use of such terminology should be construed as illustrative rather than limiting, as any suitable programming technique can be used to implement the present invention. The
5 ATS model is based on two main classes (i.e., data structures with certain attached methods): Item Specification (IS) and Adaptive Trade Specification (ATS). We first describe item specifications.

Item-Specification (IS) is a class (i.e., a data structure with attached methods). Objects
10 in this class (i.e., specific instances of the class data structure) can represent any "items" relevant in trade, such as material items (e.g., paper, electronic component, chemical), services (e.g., mail delivery, transportation, consulting time), money items (e.g., US dollars, French Francs etc.) or securities (e.g., stocks, bonds, etc.). Generally, an IS object may describe any "tradable item" that can have an associated quantity or amount.

15 Many different implementations (i.e., in terms of exact attributes and methods) of the IS class are possible. The preferred embodiment provides two implementations. However, many other implementations are also possible, such as item specifications based on ontology hierarchies as well as a variety of emerging XML-based product description standards. The
20 ATS model and the matchmaking optimization methods will work with any given IS class implementation, under the condition that the following binary Boolean function is also provided:

Give-Take-Item-Match(IS1, IS2)

Given two item specification objects *IS1* and *IS2*, *Give-Take-Item-Match(IS1, IS2)*
returns TRUE if and only if the *IS1* satisfies the requirements of *IS2*; and it returns FALSE
25 otherwise. Intuitively, this means that if a trader who requests an item with the specification

IS2 is given an item with the specification *IS1* instead, she will be satisfied. For example, if the specification *IS2* describes “any resistor with resistance between .45 to .55 ohm” and *IS1* describes a “specific resistor of a particular vendor with resistance .51 ohm”, *IS1* will satisfy the requirements of *IS2*. It is required that every implementation of the Boolean function

5 *Give-Take-Item-Match* defines the so-called *partial ordering*, that is, the following three properties must be satisfied:

- a) For every item specification object *IS*, *Give-Take-Item-Match(IS,IS)* must return TRUE.
- b) For every item specification objects *IS1* and *IS2*, if *GiveTakeItemMatch(IS1,IS2)* and
 10 *Give-Take-Item-Match(IS2,IS1)* both return TRUE, then *IS1* and *IS2* must be equivalent (i.e., traders would not distinguish them).
- c) For every item specification objects *IS1*, *IS2* and *IS3*, if *Give-Take-Item-Match(IS1,IS2)* and *Give-Take-Item-Match(IS2,IS3)* both return TRUE, then *Give-Take-Item-Match(IS1,IS3)* must also return TRUE.

15 *Item Specifications with Numeric and Non-Numeric Properties*

This is a possible implementation of the Item-Specification (IS) class. In this implementation, the IS class contains the following attributes:

1. *Non-Numeric-Properties*, which are composed of:
 - a. A set *S* of attribute names, e.g., “vendor”, “component-type”, “color”, “catalog
 20 ID” etc.
 - b. A mapping that associates, with each attribute name in *S*, its corresponding value. For example, “supplier” can be mapped to “DGK”, “component-type” to “resistor”, “color” to “black”, and “catalog ID” to “Z123-74-A45”.
2. *Numeric-Properties*, which are composed of:

a. A set of variables' (unknowns') names. e.g., "resistance", "temperature", "voltage", etc.

b. A mapping that associates, with each variable v , a range constraint of the form $Lower-bound \leq v \leq Upper-bound$. For example, $0.11 \leq resistance \leq 0.12$, $32 \leq temperature \leq 106$, or $210 \leq voltage \leq 230$.

The Boolean function *Give-Take-Item-Match*(*IS1*, *IS2*) is implemented as follows. It returns TRUE if and only if the following conditions hold:

a. Every (non-numeric) attribute name *Attr* in *IS2* appears also in *IS1*; and the value associated with *Attr* in *IS1* equals to the value associated with *Attr* in *IS2*.

b. Every (numeric) variable name *Var* in *IS2* appears also in *IS1*; and the range associated with *Var* in *IS1* must contain the range associated with *Var* in *IS2*.

For example, suppose *IS2* has non-numeric properties *component-type* = "resistor", *color* = "black" and a numeric property $0.09 \leq resistance \leq 0.12$; and *IS1* has non-numeric properties *component-type* = "resistor", *color* = "black", *catalog-ID* = "Z123-74-A45", and numeric properties $0.1 \leq resistance \leq 0.11$ and $210 \leq voltage \leq 230$. In this case *IS1* satisfies the requirements of *IS2*, and thus *Give-Take-Item-Match*(*IS1*, *IS2*) must return TRUE. Whereas, if *IS1* did not have property "color", then *Give-Take-Item-Match*(*IS1*, *IS2*) would return FALSE, which would also be the case if the non-numeric attribute "color" were mapped to "red", or if the numeric variable "resistance" were mapped to the range constraint $0.1 \leq resistance \leq 0.15$.

The above implementation of the *Give-Take-Item-Match* function defines a partial ordering, as required.

Simple Item Specifications

This is the most basic implementation of the Item-Specification (IS) class. In this implementation, the IS class contains a single attribute *Item-ID*. In this case, the function

GiveTakeItemMatch(IS1,IS2) is implemented in such a way that it returns TRUE if and only if *IS1* and *IS2* are identical. Of course, for this implementation, *Give-Take-Item-Match* defines a partial ordering, as required.

An ATS is a class (i.e., a data structure with attached methods) that consists of the
 5 following attributes:

1. *Give-Item-Entries*
2. *Take-Item-Entries*
3. *Constraints*
4. *Objective*

10 *Give-Item-Entries and Take-Item-Entries.*

Give-Item-Entries and Take-Item-Entries describe item specifications (IS) of items a trader is willing to give and take, respectively. Both Give-Item-Entries and Give-Item-Entries are of the same class (type) Item-Entries-Class, which has the following attributes:

1. A set *Item-Specs* of item specifications (*IS*).
- 15 2. A mapping that associates a *quantity-range* with each item specification (*IS*) in the set *Item-Specs*. A quantity range is a constraint of the form $Lower-bound[IS] \leq Quantity[IS] \leq Upper-bound[IS]$, which indicates that the quantity (or amount) of items corresponding to the item specification *IS* (denoted as $Quantity[IS]$) must be at least $Lower-bound[IS]$ and at most $Upper-bound[IS]$. $Lower-bound[IS]$ must be a non-negative numeric value, and
 20 $Upper-bound[IS]$ must be either a non-negative numeric value or *Infinity*, meaning that no upper bound is requested. The particular case when $Lower-bound[IS] = Upper-bound[IS]$ indicates that a fixed amount is requested. Also, each *quantity range* has an indication whether the $Quantity[IS]$ must be a integer (i.e., a whole number, such as 3 or 15) or any real number (e.g., 3.57 or 17.3894). The system must guarantee that object identifiers *IS* for each

item specification is unique, and thus the corresponding variable *Quantity[IS]* is unique for that item specification.

Constraints

Constraints is an object of type *Constraint-Class*, which is a class (i.e., a data structure and attached methods) used to describe various mathematical restrictions on numeric parameters (variables) relevant to an ATS. Before giving a precise description of the *Constraint-Class*, we explain intuitively the notion of (numerical) constraints. As an example, the expression

$$50 \leq \text{Quantity}[IS] \leq 150$$

is a (range) constraint of the kind used before. Or,

$$\text{Total-Price} = 3.4 * \text{Quantity}[IS1] + \dots + 15.7 * \text{Quantity}[ISn]$$

is a constraint that defines the function *Total-Price* as the sum of all prices of the items *IS1* through *ISn*.

As a more complex example, a reseller may have the following constraint:

$$\text{Total-Price} = \text{Unit-Price}[IS1] * \text{Quantity}[IS1] + \dots + \text{Unit-Price}[ISn] * \text{Quantity}[ISn] \text{ AND}$$

$$\text{Total-Cost} = \text{Unit-Cost}[IS1] * \text{Quantity}[IS1] + \dots + \text{Unit-Cost}[ISn] * \text{Quantity}[ISn]$$

AND

$$\text{Profit} = \text{Total-Price} - \text{Total-Cost} \text{ AND}$$

$$\text{Minimal-Profit-Margin} = 0.25 \text{ AND}$$

$$\text{Availability} = 3 \text{ (business days) AND}$$

$$\text{Profit} \geq \text{Minimal-Profit-Margin} * \text{Total-Cost} \text{ AND}$$

$$(\text{Profit} \geq 15,000$$

OR

$$\text{Total-Price} \geq 300,000$$

This constraint defines *Total-Price* and *Total-Cost* (in terms of individual quantities and unit prices and costs, respectively), *Profit*, *Minimal-Profit-Margin*, and *Availability*. Also, the constraint sets a restriction on *Profit* (to make at least the *Minimal-Profit-Margin*), and also requests that either (1) a *Profit* be at least \$15,000 (possibly above the minimal profit margins) or (2) the overall revenue (i.e., *Total-Price*) be at least \$300,000 (and still the minimal profit margin is achieved).

Some of the parameters (variables) in the above constraint, such as *Unit-Prices*, *Profit*, *Minimal-Profit-Margin*, while relevant to a supplier, may not be relevant to potential buyers. Moreover, a supplier may be willing not to disclose information about them, and decide that information to be disclosed to potential buyers could only involve *Total-Price*, *Availability*, and the quantities *Quantity[IS1]*, ..., *Quantity[ISn]*. This is done by the so-called *existential quantification* such as in:

There exist values for all variables except
 (*Total-Price*, *Availability*, *Quantity[IS1]*, ..., *Quantity[ISn]*) such that:
 (

$$\text{Total-Price} = \text{Unit-Price}[\text{IS1}] * \text{Quantity}[\text{IS1}] + \dots + \text{Unit-Price}[\text{ISn}] * \text{Quantity}[\text{ISn}]$$
 AND

$$\text{Total-Cost} = \text{Unit-Cost}[\text{IS1}] * \text{Quantity}[\text{IS1}] + \dots + \text{Unit-Cost}[\text{ISn}] * \text{Quantity}[\text{ISn}]$$
 AND

$$\text{Profit} = \text{Total-Price} - \text{Total-Cost}$$
 AND

$$\text{Minimal-Profit-Margin} = 0.25$$
 AND

$$\text{Availability} = 3 \text{ (business days)}$$
 AND

$$\text{Profit} \geq \text{Minimal-Profit-Margin} * \text{Total-Cost}$$
 AND
 ($\text{Profit} \geq 15,000$

OR

$Total-Price \geq 300,000$

)

)

5 We now give a precise description of the *Constraint-Class*. Each object of this class (including *Constraints* in the *ATS* class) has the following attributes and methods:

1. A set *Vars* of variable names (unknowns), such as *Quantity[IS]*, *Total-Price*, *Profit*, *Item-Price[IS]* etc.
2. Indication for each variable name in *Var* whether it stands for *Integer* values only, or for
10 arbitrary *Real* values.
3. A Boolean method *Truth-Value*. When applied to a *Constraint* object with argument of the class *Variable-Instantiation*, it returns a *Boolean* value TRUE or FALSE. An object of the class *Variable-Instantiation* stores an integer value for each *Integer* variable in the constraint, and real value for each *Real* variable. For example, given a *Variable-*
15 *Instantiation* of 3 to *x* and 4 to *y*, the *Truth-Value* of the constraint $x + y \leq 6$ is FALSE because it is not correct that $3 + 4 \leq 6$. On the other hand, for the *Variable-Instantiation* of 2 to *x* and 3 to *y*, the *Truth-Value* of the constraint $x + y \leq 6$ is TRUE, because it is correct that $2 + 3 \leq 6$.
4. A Boolean method *Satisfiable* with no arguments. When applied to a *Constraint* object, it
20 returns the *Boolean* value TRUE if and only if there exists a *Variable-Instantiation* that makes the *Constraint* object TRUE (i.e., *Truth-Value* method applied to the *Constraint* object with the argument *Variable-Instantiation* would return TRUE.). For example, the constraint $x + y \leq 6$ is *Satisfiable* because there exist a *Variable-Instantiation* (e.g., 2 to *x* and 3 to *y*) that makes the constraint TRUE.

25 *Objective*

Objective is an object of the class *Objective-Class*, which has two attributes:

1. *Objective-Function*, which is a name of a parameter (variable) to be optimized (e.g., *Profit*, *Total-Cost*)
2. Indication whether *Minimum* or *Maximum* of the objective function is desired (by the
5 trader).

Note the definition of the objective function (e.g., $Profit = Total-Price - Total-Cost$ etc.) is given in *Constraints*.

FIG. 3 provides a high level graphical description of the classes Item Specification and Adaptive Trade Specification. An ATS class 301 includes four components: give-item-
10 entries 303, take-item-entries 305, constraints 307 and an objective 309. The give-item-entries 303 identify what the particular user is willing to give in the trade and include one or more item specifications 311. The take-item-entries 305 identify what the user wants in return and include one or more item specifications 313. The constraints 307 set forth restrictions that must be satisfied before a transaction can be carried out, e.g., constraints on
15 quantity or on time of delivery. The objective 309 indicates what the particular user wants to optimize; for example, a seller may want to optimize (maximize) profit, while a buyer may want to optimize (minimize) total cost.

ATS-based match-making (MM) optimization methods will now be explained.

Given a trader's ATS, the MM Optimization methods recommend specific
20 transactions with other traders (i.e., against their ATS's) that are mutually agreeable and optimize the objective of the trader's ATS (e.g., minimal price, maximal profit etc.). The recommended set of transactions will indicate exactly with whom the transaction should be made, the exact GIVE and TAKE items and their quantities, as well as other relevant parameters (e.g., price and profit). For example, for procurement ATS, the MM optimization
25 methods can recommend a set of suppliers ATS's and the exact quantities of the items to be

purchased from each, so that the procurement ATS objective, say the minimal total cost, is achieved. Or, for a manufacturer's ATS, the MM optimization methods can recommend a set of buyers ATS's interested in the manufacturer's products, and a set of ATS's suppliers of raw materials necessary to manufacture the products, so that the manufacturer's objective, say maximal profit, is achieved. The ATS-based match making and optimization are generic and work uniformly regardless of how or for what type of trader the input ATS's were generated (e.g., what "wizard" interface generated them).

We will now describe three methods for match-making optimization and two auxiliary methods for mathematical programming optimization and the construction of multi-match constraints.

Given Mathematical Programming Optimization Methods

The MM optimization methods use, and assume as given, two mathematical programming methods (functions):

- *Minimize(Objective-Function, Constraint)* and
- *Maximize(Objective-Function, Constraints)*

These functions find the minimum and maximum, respectively, of the objective function subject to *Constraints*. Specifically, each of the methods returns as output an object *Value-At-Point* of the class *Value-At-Point-Class*, which has two attributes:

1. *Optimal-Value* (i.e., maximum or minimum)
2. *Optimal-Variable-Instantiation*, that is, a *Variable-Instantiation* that satisfies the *Constraints*, and at which the *Optimum-Value* is achieved.

The mathematical programming methods above are provided as examples for carrying out the preferred embodiment and are not intended as limitations on the present invention. For many families of constraints, such as linear, mixed integer linear etc., commercial and freeware software packages are available that provide the functionality of the *Minimize* and

Maximize methods. As an example, CPLEX of the ILOG corporation and OSL of the IBM corporation are well-known packages for mixed integer (mathematical) programming.

FIGS. 4A-4E provide a high level graphical description of the methods outlined below. Figs. 5A-5E provide corresponding low-level descriptions.

5 **A. Method for Constructing ATS MM Constraints (Figs. 4A and 5A)**

Method (403) Name: *Construct-ATS-MM-Constraints* ($\{A1, A2, \dots, An\}$)

Input (401): A set $\{A1, A2, \dots, An\}$ of ATS's.

Output (405): *Constraints* that express the fact that ATS's in $\{A1, A2, \dots, An\}$ are mutually agreeable.

10 **Algorithm Description:**

Step 501. Construct *Original-ATS-Constraints* as

Constraints of *A1* AND

Constraints of *A2* AND

... AND

15 *Constraints* of *An*.

Step 503. Construct *Give-Quantity-Constraints* as follows:

a. Initially, set *Give-Quantity-Constraints* to the empty conjunction (logical AND) of constraints,

i.e. a constraint that is equivalent to TRUE.

20 b. For each ATS *A* from the set $\{A1, \dots, An\}$ and

For each item specification *IS* from *Give-Item-Entries* of *A* do:

Set *Give-Quantity-Constraints* to

Give-Quantity-Constraints AND *quantity-range* of *IS*

(note, the latter is $\text{Lower-bound}[IS] \leq \text{Quantity}[IS] \leq \text{Upper-bound}[IS]$)

25 Step 505. Construct *Take-Quantity-Constraints* as follows:

- a. Initially, set *Take-Quantity-Constraints* to the empty conjunction (logical AND) of constraints,
i.e. a constraint that is equivalent to FALSE.
- b. For each ATS *A* from the set $\{A1, \dots, An\}$ and
- 5 For each item specification *IS* from *Take-Item-Entries* of *A* do:
Set *Take-Quantity-Constraints* to
Take-Quantity-Constraints AND *quantity-range* of *IS*
(Note: the latter is $\text{Lower-bound}[IS] \leq \text{Quantity}[IS] \leq \text{Upper-bound}[IS]$)
- Step 507. Construct the set *All-Give-Item-Specs* as follows:
- 10 a. Set *All-Give-Item-Specs* to the empty set
- b. For each ATS *A* from the input set $\{A1, \dots, An\}$ of ATS's do:
Set *All-Give-Item-Specs* to *All-Give-Item-Specs* union *Item-Specs*,
where *Item-Specs* is the set of all item specifications in *Give-Item-Entries* of the ATS
A.
- 15 Step 509. Construct the set *All-Take-Item-Specs* as follows:
- a. Set *All-Take-Item-Specs* to the empty set.
- b. For each ATS *A* from the input set $\{A1, \dots, An\}$ of ATS's do:
Set *All-Take-Item-Specs* to *All-Take-Item-Specs* union *Item-Specs*,
where *Item-Specs* is the set of all item specifications in *Take-Item-Entries* of the ATS
A.
- 20 *A*.
- Step 511. For each item specification *tIS* from *All-Take-Item-Specs* and
For each item specification *gIS* from *All-Give-Item-Specs* such that
Give-Take-Item-Match(*gIS*, *tIS*) = TRUE (i.e., *gIS* satisfies the requirements of *tIS*) do:
Create a new quantity variable *Quantity*[*gIS*, *tIS*].
- 25 (Note: *Quantity*[*gIS*, *tIS*] expresses the quantity of *gIS* given toward the

required quantity of tIS)

Step 513. Construct *Take-Zero-Sum-Constraints* as follows:

For each item specification tIS from *All-Take-Item-Specs* do:

a. Set *Zero-Sum-Constraints*[tIS] to

$$5 \quad \text{Quantity}[tIS] = \text{Quantity}[gIS-1, tIS] + \dots + \text{Quantity}[gIS-n, tIS]$$

where $gIS-1, \dots, gIS-n$ are all item specification from *All-Give-Item-Specs* that are satisfied by the item specification tIS (i.e., $\text{Give-Take-Item-Match}(gIS-I, tIS) = \text{TRUE}$ for every $I = 1, \dots, n$)

b. Set *Take-Zero-Sum-Constraints* to

$$10 \quad \text{Zero-Sum-Constraints}[tIS-1] \text{ AND } \dots \text{ AND } \text{Zero-Sum-Constraints}[tIS-m]$$

where $tIS-1, \dots, tIS-m$ are all item specifications from *All-Take-Item-Specs*.

Step 515. Construct *Give-Zero-Sum-Constraints* as follows:

For each item specification tIS from *All-Give-Item-Specs* do:

a. Set *Zero-Sum-Constraints*[gIS] to

$$15 \quad \text{Quantity}[gIS] = \text{Quantity}[gIS, tIS-1] + \dots + \text{Quantity}[gIS, tIS-m]$$

where $tIS-1, \dots, tIS-m$ are all item specification from *All-Take-Item-Specs* that satisfy the item specification gIS (i.e., $\text{Give-Take-Item-Match}(gIS, tIS-I) = \text{TRUE}$ for every $I = 1, \dots, m$)

b. Set *Give-Zero-Sum-Constraints* to

$$20 \quad \text{Zero-Sum-Constraints}[gIS-1] \text{ AND } \dots \text{ AND } \text{Zero-Sum-Constraints}[gIS-n]$$

where $gIS-1, \dots, gIS-n$ are all item specifications from *All-Give-Item-Specs*.

Step 517. Construct *Constraints* as

Original-Constraints AND

Give-Quantity-Constraints AND

25 *Take-Quantity-Constraints* AND

Give-Zero-Sum-Constraints AND

Take-Zero-Sum-Constraints

Step 519. Return *Constraints* as output.

End of Method.

5 **Generic Multiple MM Optimization Method (Figs. 4B and 5B)**

Method (407) Name: *ATS-Multiple-MM-Optimization({A1,...,An}, Objective, Additional-Constraints)*

Input (409):

1. A set $\{A1, ..., An\}$ of ATS's (411)
- 10 2. *Objective* of the class *Objective-Class* (recall: it includes an *Objective-Function* and an indication whether minimum or maximum is sought. (413)
3. *Additional-Constraints*, which can be used to describe additional interrelationships among numeric variables in different ATS's in $\{A1, ..., An\}$. (415)

Output (417):

- 15 1. An *Optimal-Variable-Instantiation* into all variables that appear in *MM-Constraints*($\{A1, ..., An\}$) (including quantities of all item specifications) that achieves the optimal objective of the *Optimizing-ATS*. (419)
2. The *Optimal-Value* for the *Objective-Function* for the *Optimal-Variable-Instantiation*. (421)
- 20 3. A set *Winning-ATS-set* of winning filtered ATS's from *Committed-ATS-Set* in which all items specifications *IS* with $Quantity[IS] = 0$ are eliminated. Also eliminated from *Winning-ATS-Set* are all ATS's in which both *Give-Item-Entries* and *Take-Item-Entries* became empty, after item specification with zero quantities were eliminated. (423)

Algorithm Description:

Step 521. Construct *MM-Constraints* by applying the method *Construct-ATS-MM-Constraints* ($\{A1, \dots, An\}$) on the input set of ATS's $\{A1, \dots, An\}$.

Step 523. Construct *Combined-Constraints* as
MM-Constraints AND Additional-Constraints

5 Steps 525-529. If *Objective* indicates that minimum is sought (step 525), apply the method *Minimize*(*Objective-Function*, *Combined-Constraints*) (step 527) that returns the optimal *Value-At-Point* (Recall: it has the attributes *Optimal-Value* of the type *Real* and *Optimal-Point* of the class *Variable-Instantiation-Class*). Otherwise, if *Objective* indicates that maximum is sought, apply the method *Maximize*(*Objective-Function*, *Combined-*
 10 *Constraints*) (step 529) that returns the optimal *Value-At-Point*. (Recall: it has the attributes *Optimal-Value* of the type *Real* and *Optimal-Variable-Instantiation* of the class *Variable-Instantiation-Class*).

Step 531. Initialize *Winning-ATS-Set* as $\{A1, \dots, An\}$.

Step 533. For every ATS *A* in *Winning-ATS-Set* do:

15 a. For every item specification *IS* in *Give-Item-Entries* of *A* do:
 If *Quantity[IS]* is instantiated to 0 by the variable instantiation *Value-At-Point* then
 Delete *IS* from *Give-Item-Entries* and the related mapping to *Quantity-Ranges*
 b. For every item specification *IS* in *Take-Item-Entries* of *A* do:
 If *Quantity[IS]* is instantiated to 0 by the variable instantiation *Value-At-Point* then
 20 Delete *IS* from *Give-Item-Entries* and the related mapping to *Quantity-Ranges*
 c. If both *Give-Item-Entries* and *Take-Item-Entries* of *A* become empty after deletion of item specifications in steps a. and b., then delete *A* from *Winning-ATS-Set*.

Step 535. Return as output:

a. *Optimal-Variable-Instantiation* which is the *Variable-Instantiation* which was
 25 returned in *Value-At-Point*.

- b. The *Optimal-Value* which was returned in *Value-At-Point*.
- c. *Winning-ATS-Set*

End of method.

One-to-All MM Optimization Method (Figs. 4C and 5C)

5 **Method (425) Name:** *ATS-One-to-All-MM-Optimization*(*{Optimizing-ATS, Committed-ATS-Set}*)

Input (427):

1. *Optimizing-ATS*, which is an ATS whose *Objective* will be used for optimization. (429)
2. *Committed-ATS-Set*, which is a set of ATS's that are committed to perform a transaction
- 10 if and only if their *Constraints* are satisfied. The *Objectives* of the committed ATS's are not used in optimization. (431)

Output (433):

1. An *Optimal-Variable-Instantiation* into all variables that appear in *MM-Constraints*(*{Optimizing-ATS}* union *Committed-ATS-Set*) (including quantities of all item
- 15 specifications) that achieves the optimal objective of the *Optimizing-ATS*. (435)
2. The *Optimal-Value* for the *Objective-Function* for the *Optimal-Variable-Instantiation*. (437)
3. A set *Winning-ATS-set* of winning filtered ATS's from *Committed-ATS-Set* in which all items specifications *IS* with $Quantity[IS] = 0$ are eliminated. Also eliminated from *Winning-*
- 20 *ATS-Set* are all ATS's in which both *Give-Item-Entries* and *Take-Item-Entries* became empty after item specifications with zero associated quantity were eliminated. (439)

Algorithm Description:

Step 541. Set *ATS-Set* to the union of *Committed-ATS-Set* and the singleton set *{Optimizing-ATS}*

25 Step 543. Set *Objective* to the objective of *Optimizing-ATS*

Step 545. Set *Additional-Constraints* to the empty conjunction of constraints, i.e., the constraint equivalent to TRUE.

Step 547. Apply the method *ATS-Multiple-MM-Optimization(ATS-Set, Objective, Additional-Constraints)* to compute *Optimal-Variable-Instantiation*, *Optimal-Value* and
 5 *Winning-ATS-Set*.

Step 549. Return *Optimal-Variable-Instantiation*, *Optimal-Value* and *Winning-ATS-Set* as output.

End of Method

One-to-One MM Optimization Method (Figs. 4D and 5D)

10 **Method (441) Name:** *One-to-One-MM-Optimization({Optimizing-ATS, Committed-ATS-Set})*

Input (443):

1. *Optimizing-ATS*, which is an ATS whose *Objective* will be used for optimization. (445)
2. *Committed-ATS-Set*, which is a set of ATS's that are committed to perform a transaction
 15 if and only if their *Constraints* are satisfied. The *Objectives* of the committed ATS's are not used in optimization. (447)

Output (449):

1. *Winning-ATS*, from *Committed-ATS-Set*, which is recommended for making a deal with. All item specifications *IS* with $Quantity[IS] = 0$ (in *Optimal-Variable-Instantiation*
 20 below) are deleted. (451)
2. An *Optimal-Variable-Instantiation* into all variables that appear in *MM-Constraints({Optimizing-ATS, Winning-ATS})* (including quantities of all item specifications) that achieves the optimal objective of the *Optimizing-ATS*. (453)
3. The *Optimal-Value* of the *Objective-Function* for the *Optimal-Variable-Instantiation*.
 25 (455)

Algorithm Description:

A. If the *Objective* of the *Optimizing-ATS* requires minimum, do:

Step 551. Set *Current-Minimum* to *+ infinity*

Step 553. Set *Current-Variable-Instantiation* to null (i.e., undefined).

5 Step 555. Set *Winning-ATS* to null (i.e., undefined).

For each ATS *A* in *Committed-ATS-Set* do:

Step 557. Apply *ATS-Multiple-MM-Optimization* on the set $\{\textit{Optimizing-ATS}, A\}$ of ATS's, the *Objective* of *Optimizing-ATS*, and the empty *Additional-Constraints*.

10 Steps 559-565. If the returned *Optimal-Value* < *Current-Minimum*, as determined in step 559, do:

Step 561. Set *Current-Minimum* to *Optimal-Value*;

Step 563. Set *Current-Variable-Instantiation* to the returned *Optimal-Variable-Instantiation*.

15 Step 565. Set *Winning-ATS* to the current ATS *A*.

Step 567. Return as output:

Winning-ATS

Current-Variable-Instantiation as *Optimal-Variable-Instantiation*

Current-minimum as *Optimal-Value*.

20 B. If the *Objective* of the *Optimizing-ATS* requires maximum, do:

Step 551. Set *Current-Maximum* to *- infinity*

Step 553. Set *Current-Variable-Instantiation* to null (i.e., undefined).

Step 555. Set *Winning-ATS* to null (i.e., undefined).

For each ATS *A* in *Committed-ATS-Set* do:

Step 557. Apply *ATS-Multiple-MM-Optimization* on the set $\{\text{Optimizing-ATS}, A\}$ of ATS's, the *Objective* of *Optimizing-ATS*, and the empty *Additional-Constraints*.

Steps 559-565. If the returned *Optimal-Value* > *Current-Minimum*, as determined in step 559, do:

Step 561. Set *Current-Maximum* to *Optimal-Value*;

Step 563. Set *Current-Variable-Instantiation* to the returned *Optimal-Variable-Instantiation*.

Step 565. Set *Winning-ATS* to the current ATS *A*.

Step 567 Return as output:

Winning-ATS

Current-Variable-Instantiation as *Optimal-Variable-Instantiation*

Current-Maximum as *Optimal-Value*.

End of Method

One-to-K MM Optimization Method (Figs. 4E and 5E)

Method (457) Name: *ATS-One-to-K-MM-Optimization*($\{\text{Optimizing-ATS}, \text{Committed-ATS-Set}\}$)

Input (459):

1. *Optimizing-ATS*, which is an ATS whose *Objective* will be used for optimization. (461)

2. *Committed-ATS-Set*, which is a set of ATS's that are committed to perform a transaction if and only if their *Constraints* are satisfied. The *Objectives* of the committed ATS's are not used in optimization. (463)

Output (465):

1. An *Optimal-Variable-Instantiation* into all variables that appear in *MM-Constraints* ($\{ \textit{Optimizing-ATS} \}$ union *Winning-ATS-Set*) (including quantities of all item specifications) that achieves the optimal objective of the *Optimizing-ATS*. (467)

2. The *Optimal-Value* for the *Objective-Function* for the *Optimal-Variable-Instantiation*.

5 (469)

3. *Winning-ATS-set* of at most K winning filtered *ATS*'s from *Committed-ATS-Set* in which all items specifications *IS* with $\textit{Quantity}[IS] = 0$ are eliminated. Also eliminated from *Winning-ATS-Set* are all *ATS*'s in which both *Give-Item-Entries* and *Take-Item-Entries* became empty after item specifications with zero associated quantity were eliminated. (471)

10 **Algorithm Description:**

Step 571. For each K *ATS*'s $\{A1, \dots, Ak\}$ in *Committed-ATS-Set*, perform *ATS-One-to-All-MM-optimization*(*Optimizing-ATS*, $\{A1, \dots, Ak\}$).

Step 573. Among all sets $\{A1, \dots, Ak\}$, choose the one that has minimal (or maximal, as required in *Optimizing-ATS*) *Optimal-Value*.

15 Step 575. Return as output the output of *ATS-One-to-All-MM-Optimization* for the selected set $\{A1, \dots, Ak\}$ with the minimal (or maximal, as required in *Optimizing-ATS*) objective.

End of Method.

20 While a preferred embodiment of the present invention has been set forth in detail above, those skilled in the art who have reviewed the present disclosure will readily appreciate that other embodiments can be realized within the scope of the present invention. For example, disclosures of certain hardware, operating systems, and other software are illustrative rather than limiting, as are specific numerical values. Therefore, the present invention should be construed as limited only by the appended claims.

We claim:

1. A system for storing information concerning a plurality of traders, the system comprising:

(a) a database server; and

5 (b) a database stored on the database server, the database comprising a plurality of adaptive trade specifications, each of the plurality of adaptive trade specifications comprising, for one of the traders:

(i) at least one give-item entry identifying at least one item that said one of the traders is willing to give in an exchange:

10 (ii) at least one take-item entry identifying at least one item that said one of the traders wants in return for the at least one item identified in the give-item entry;

(iii) at least one constraint entry identifying at least one constraint that said one of the traders has placed on the exchange; and

15 (iv) an objective entry identifying an objective sought by said one of the traders in the exchange.

2. The system of claim 1, wherein, for at least one of the adaptive trade specifications, the objective comprises a maximization of a quantity associated with the exchange.

3. The system of claim 2, wherein the quantity is a profit resulting from the exchange.

20 4. The system of claim 1, wherein, for at least one of the adaptive trade specifications, the objective comprises a minimization of a quantity associated with the exchange.

5. The system of claim 4, wherein the quantity is a total cost of the exchange.

6. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a quantitative identification of the at least one item identified
25 in the give-item entry.

7. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a qualitative identification of the at least one item identified in the give-item entry.
8. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a quantitative and qualitative identification of the at least one item identified in the give-item entry.
9. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a quantitative identification of the at least one item identified in the take-item entry.
10. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a qualitative identification of the at least one item identified in the take-item entry.
11. The system of claim 1, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a quantitative and qualitative identification of the at least one item identified in the take-item entry.
12. The system of claim 1, further comprising an application server, in communication with the database server, for generating a match between at least two of the adaptive trade specifications in accordance with their give-item entries, take-item entries, and constraint entries to optimize the objective identified in the objective entry of at least one of the adaptive trade specifications.
13. The system of claim 12, further comprising a communication server, in communication with the database server and the application server and also in communication with the plurality of traders, for providing communication between (i) the plurality of traders and (ii) the application server and the database server.

14. The system of claim 13, wherein the communication server is in communication with the plurality of traders over the Internet.
15. The system of claim 12, wherein the objective is optimized by maximizing a quantity associated with the exchange.
- 5 16. The system of claim 12, wherein the objective is optimized by minimizing a quantity associated with the exchange.
17. The system of claim 12, wherein the application server generates a matchmaking constraint set of adaptive trade specifications having mutually agreeable give-item entries, take-item entries, and constraints and generates the match from the
10 matchmaking constraint set.
18. The system of claim 17, wherein the application server uses the matchmaking constraint set to optimize the objective.
19. The system of claim 12, wherein the application server generates the match set between (i) an adaptive trade specification which supplies the objective to be
15 optimized and (ii) a set of adaptive trade specifications.
20. The system of claim 19, wherein the match set consists of a single adaptive trade specification.
21. The system of claim 19, wherein the match set comprises a plurality of adaptive trade specifications.
- 20 22. A method for storing information concerning a plurality of traders, the method comprising:
- (a) receiving a plurality of adaptive trade specifications, each of the plurality of
adaptive trade specifications comprising, for one of the traders:
- (i) at least one give-item entry identifying at least one item that said one
25 of the traders is willing to give in an exchange:

- (ii) at least one take-item entry identifying at least one item that said one of the traders wants in return for the at least one item identified in the give-item entry;
- (iii) at least one constraint entry identifying at least one constraint that said one of the traders has placed on the exchange; and
- (iv) an objective entry identifying an objective sought by said one of the traders in the exchange; and
- (b) storing the plurality of adaptive trade specifications in a database.
23. The method of claim 22, wherein, for at least one of the adaptive trade specifications, the objective comprises a maximization of a quantity associated with the exchange.
24. The method of claim 23, wherein the quantity is a profit resulting from the exchange.
25. The method of claim 22, wherein, for at least one of the adaptive trade specifications, the objective comprises a minimization of a quantity associated with the exchange.
26. The method of claim 25, wherein the quantity is a total cost of the exchange.
27. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a quantitative identification of the at least one item identified in the give-item entry.
28. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a qualitative identification of the at least one item identified in the give-item entry.
29. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the give-item entry includes a quantitative and qualitative identification of the at least one item identified in the give-item entry.

30. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a quantitative identification of the at least one item identified in the take-item entry.
31. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a qualitative identification of the at least one item identified in the take-item entry.
32. The method of claim 22, wherein, in at least one of the adaptive trade specifications, the take-item entry includes a quantitative and qualitative identification of the at least one item identified in the take-item entry.
33. The method of claim 22, further comprising (c) generating a match between at least two of the adaptive trade specifications in accordance with their give-item entries, take-item entries, and constraint entries to optimize the objective identified in the objective entry of at least one of the adaptive trade specifications.
34. The method of claim 33, further comprising (d) providing communication between (i) the plurality of traders and (ii) the application server and the database server.
35. The method of claim 34, wherein step (d) is performed over the Internet.
36. The method of claim 33, wherein the objective is optimized by maximizing a quantity associated with the exchange.
37. The method of claim 33, wherein the objective is optimized by minimizing a quantity associated with the exchange.
38. The method of claim 33, wherein step (c) comprises generating a matchmaking constraint set of adaptive trade specifications having mutually agreeable give-item entries, take-item entries, and constraints and generating the match from the matchmaking constraint set.

39. The method of claim 38, wherein step (c) further comprises using the matchmaking constraint set to optimize the objective.
40. The method of claim 33, wherein step (c) comprises generating the match set between
- (i) an adaptive trade specification which supplies the objective to be optimized and
- 5 (ii) a set of adaptive trade specifications.
41. The method of claim 40, wherein the match set consists of a single adaptive trade specification.
42. The method of claim 40, wherein the match set comprises a plurality of adaptive trade specifications.

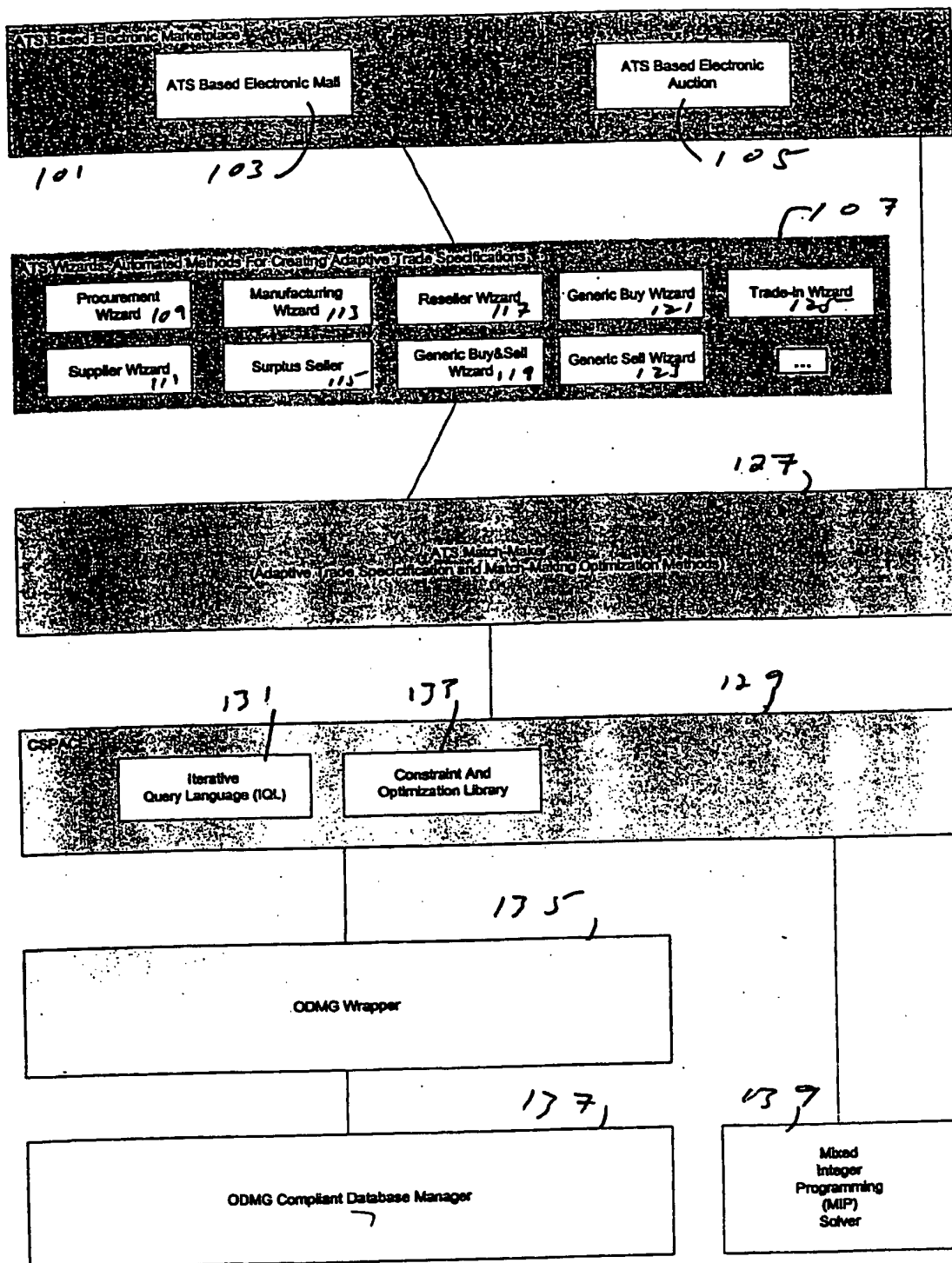


Fig. 1

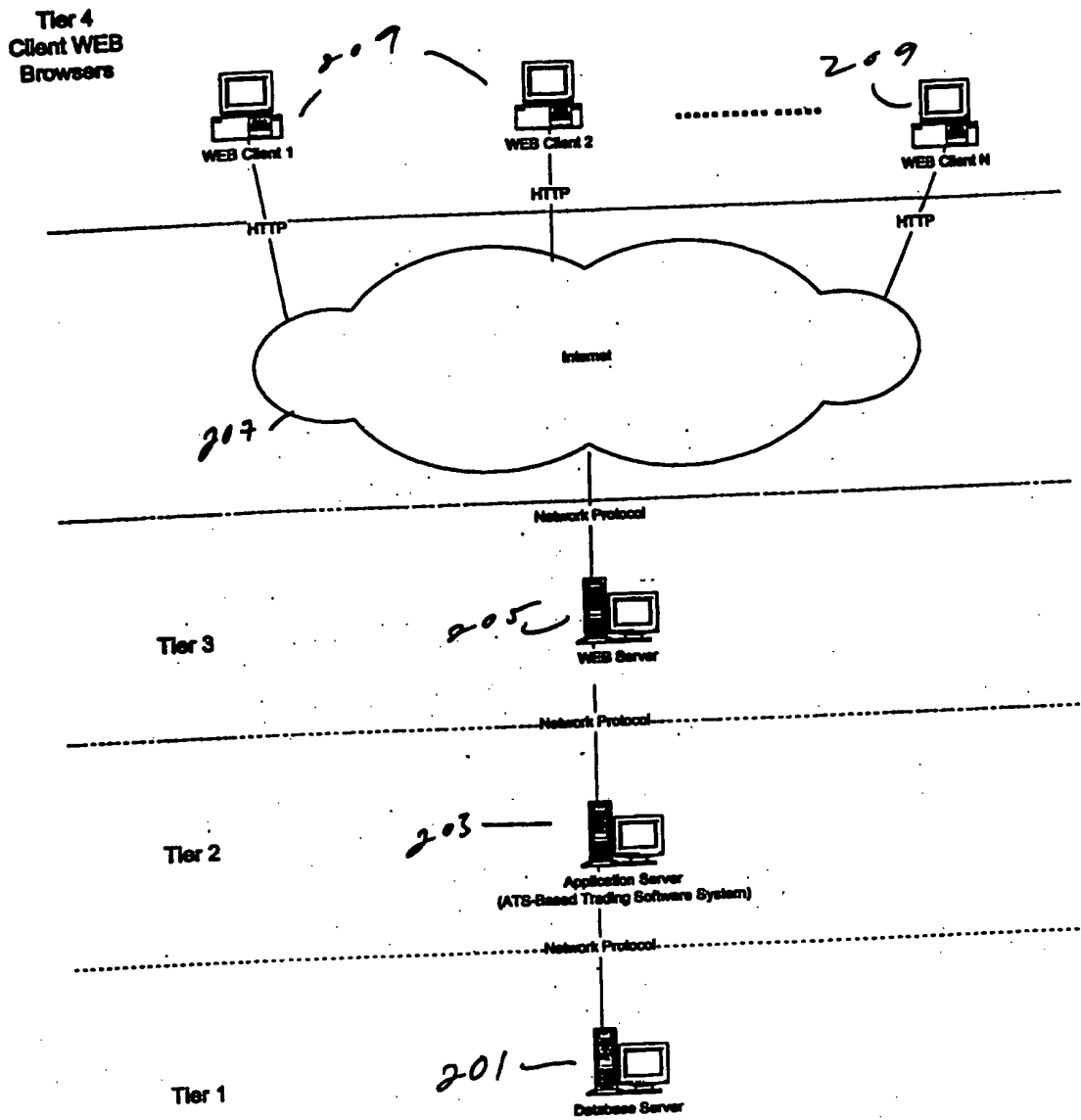


FIG. 2

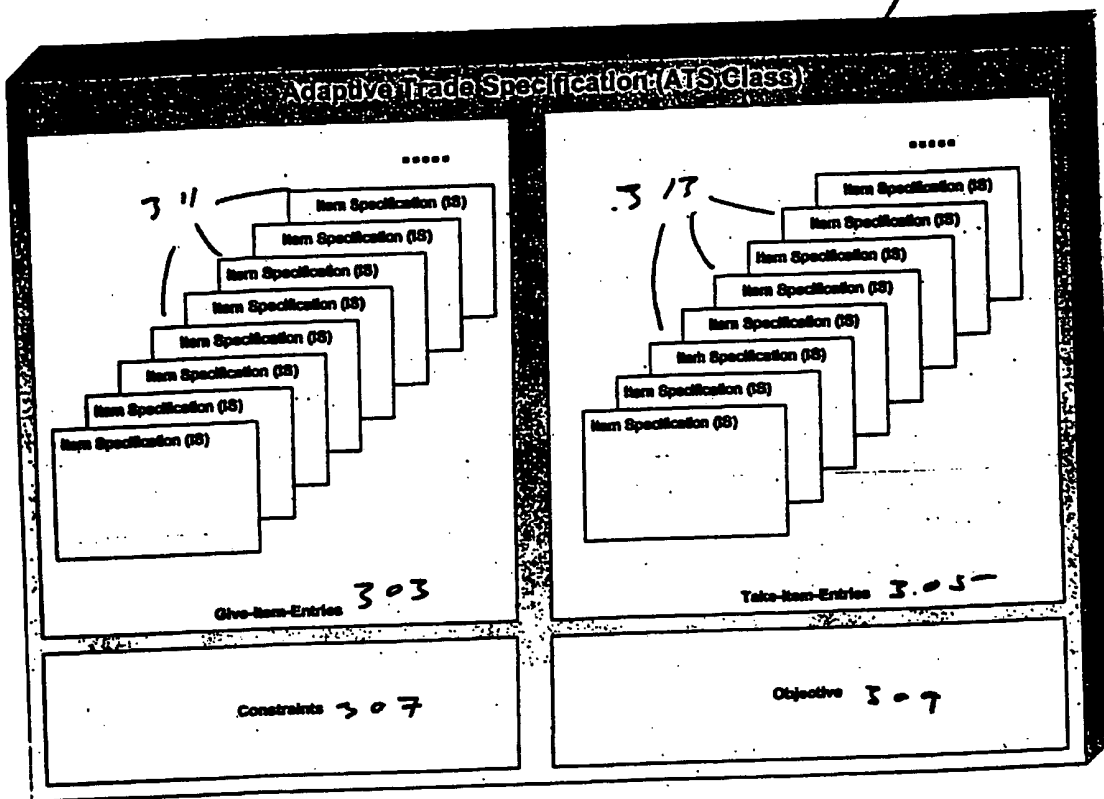


FIG. 3

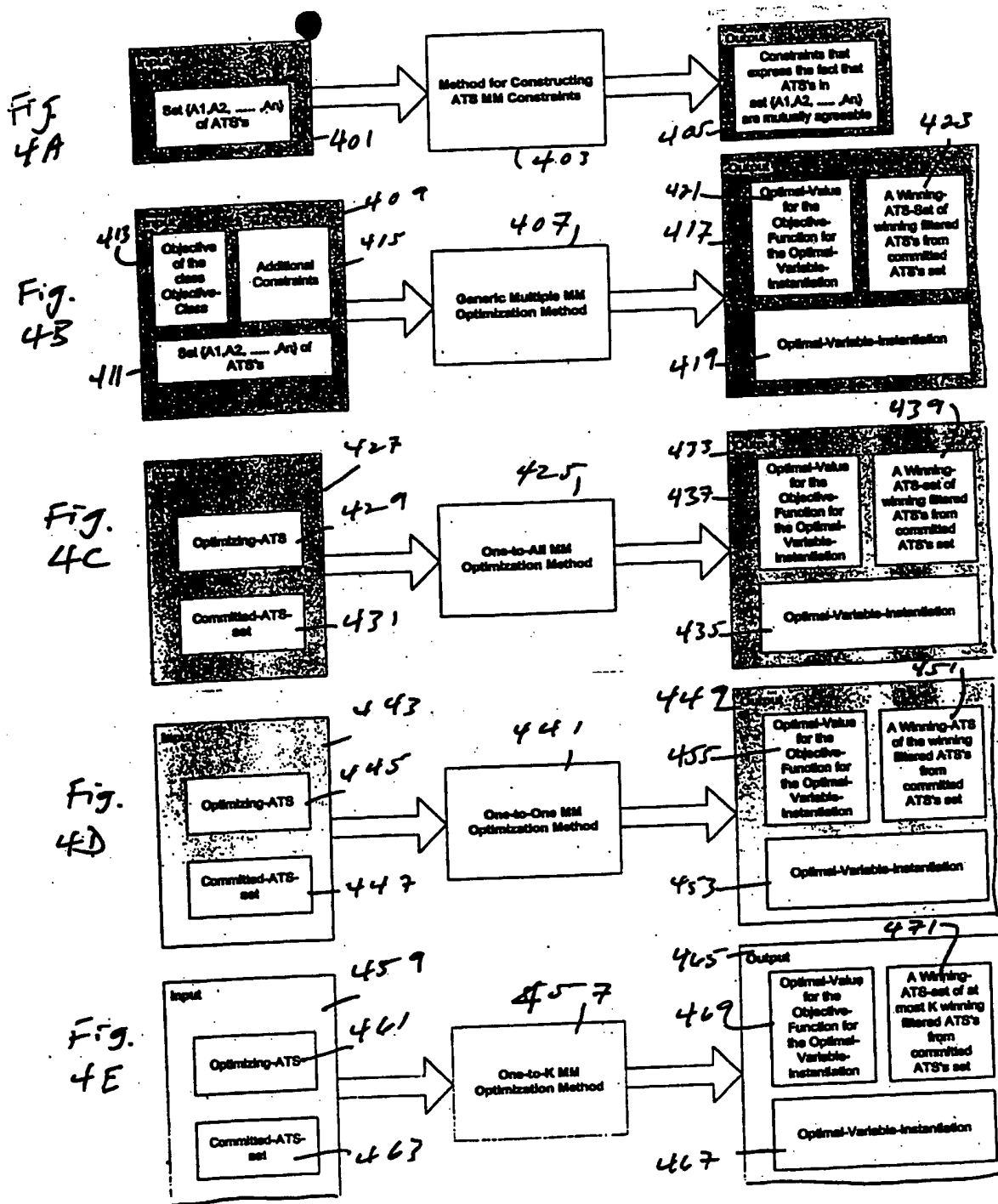


Fig. 5A

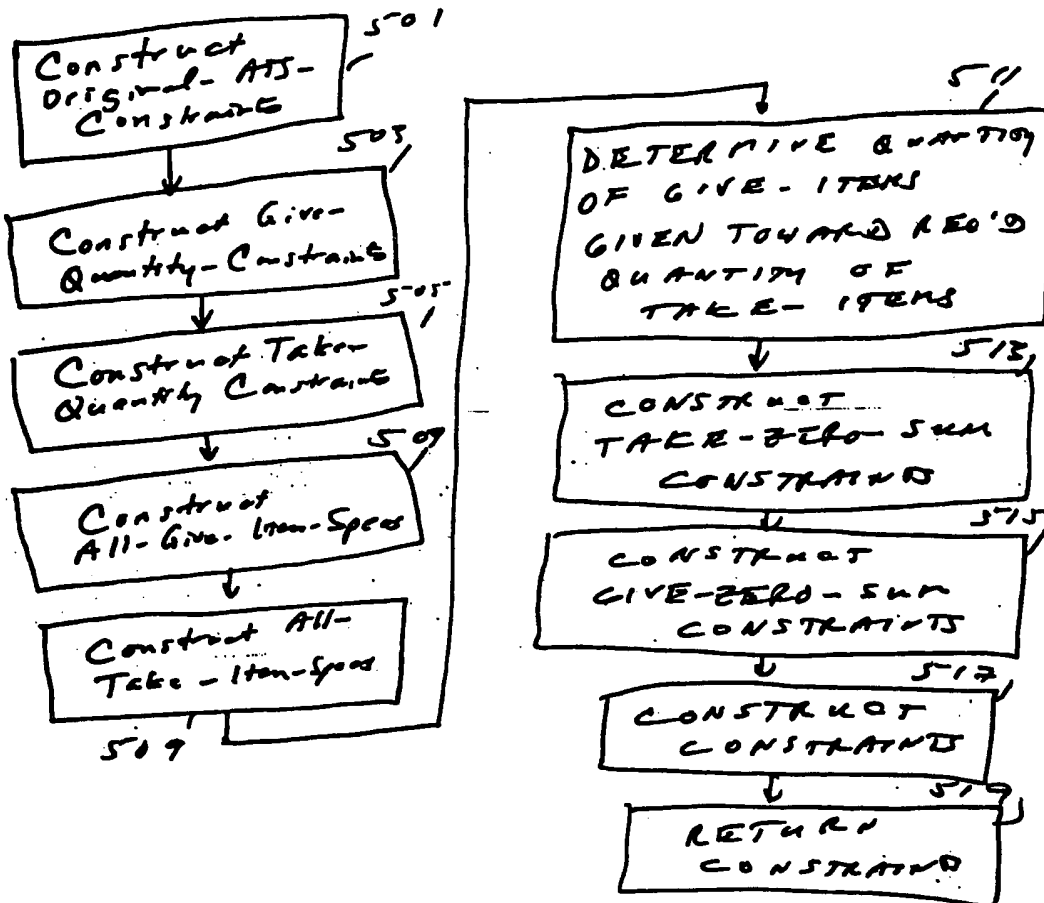


Fig. 5B

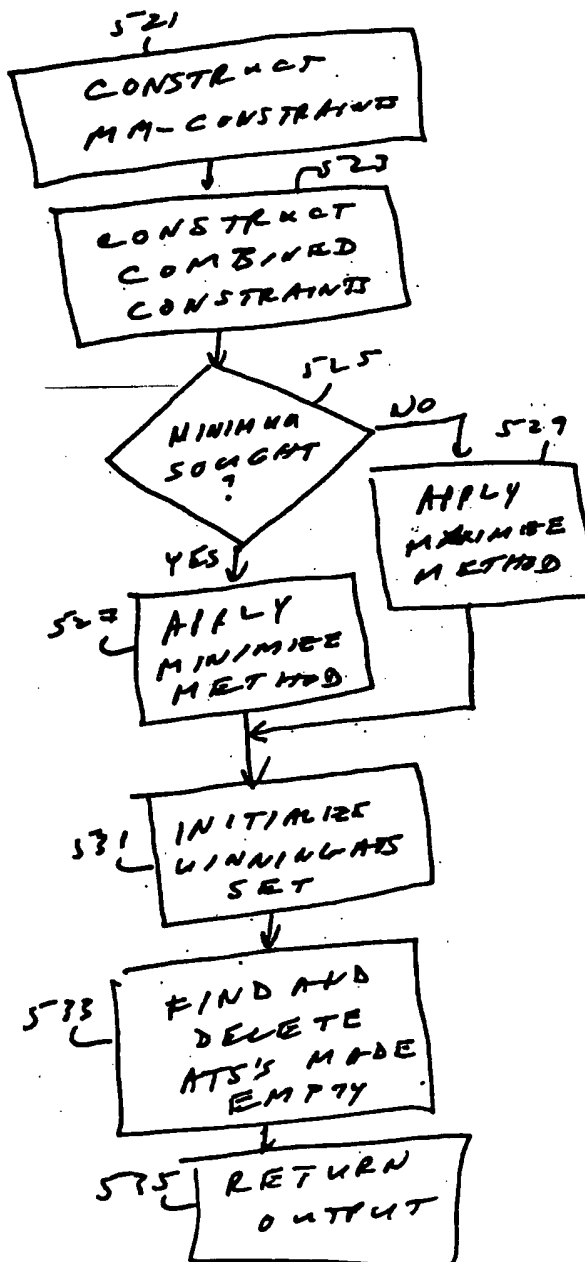


Fig. 5C

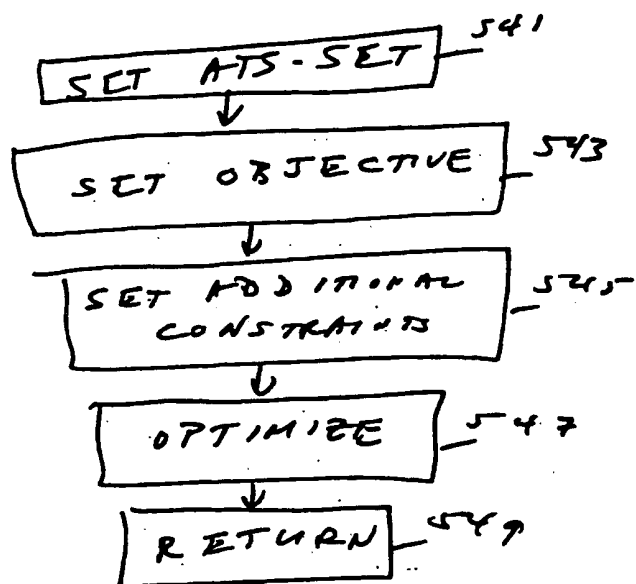


Fig. 5D

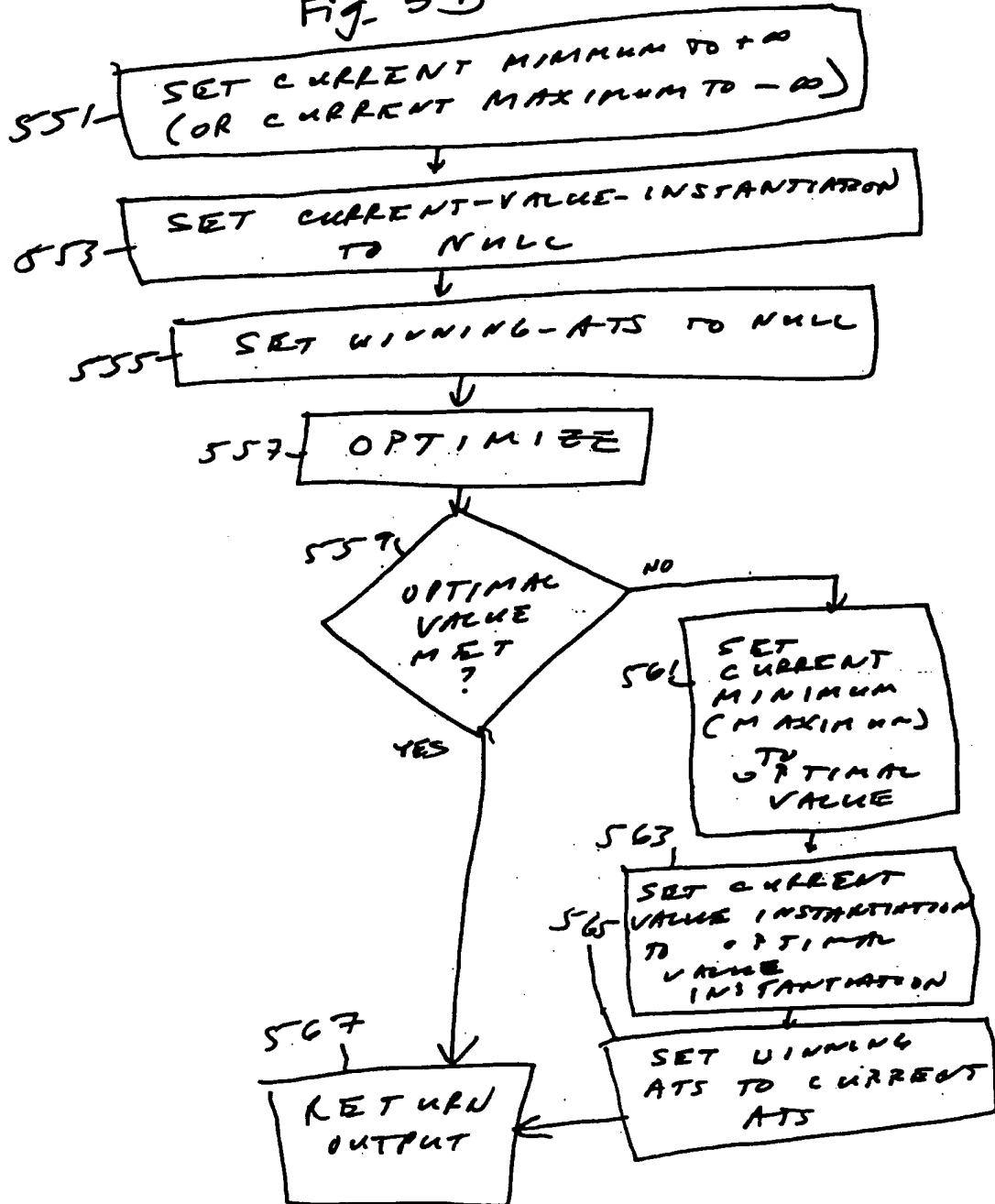


Fig. 5E

